

Discriminant

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$$\text{Quad formula } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\text{Discriminant} = b^2 - 4ac$$

if bigger than 0 \rightarrow 2 real solutions

if less than 0 \rightarrow no real solutions

if 0 \rightarrow 1 real solution

1) $x^2 + 4x - 7 = 0$

$$a=1 \quad b=4 \quad c=-7$$

$$D = b^2 - 4ac$$

$$D = (4)^2 - 4(1)(-7)$$

$$D = 44 \rightarrow \text{positive so 2 real solutions}$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \rightarrow \frac{-4 \pm \sqrt{44}}{2(1)} \rightarrow \frac{-4 \pm \sqrt{4 \cdot 11}}{2} \rightarrow \frac{-4 \pm 2\sqrt{11}}{2}$$

$$\frac{-4 \pm 2\sqrt{11}}{2} \rightarrow \frac{-4}{2} \pm \frac{2\sqrt{11}}{2} \quad x = -5.32 \text{ \& } 1.32$$

two real solutions ✓

2) $x^2 - 6x + 9 = 0$

$$D = (-b)^2 - 4(1)(9)$$

$$D = 0 \quad -1 \text{ real solution}$$

$$x = \frac{6 \pm \sqrt{(-6)^2 - 4(1)(9)}}{2(1)} \rightarrow \frac{6 \pm \sqrt{0}}{2} \rightarrow \frac{6}{2} \rightarrow \boxed{3}$$

one real solution

$$3) 2x^2 + 5x + 8 = 0$$

$$D = (5)^2 - 4(2)(8)$$

$D = -39 \rightarrow 2$ imaginary or no real solutions

$$x = \frac{-5 \pm \sqrt{-39}}{2(2)} \rightarrow \frac{-5 \pm \sqrt{-39}}{4} \rightarrow \text{not factorable}$$

ignore info about imaginary #'s. We do not cover imaginary in Alg 1.